ABSTRACT

In BASE SAS®, there are multiple logarithmic functions available. The most used log functions are the natural and common log functions. However, the syntax of the natural log function can be easily confused with the mathematical notation for the common log and can lead to incorrect results. This intent of this paper is to explore the definitions of each of these log functions, to seek out full understanding, and to boldly go where no programmer has gone before.

INTRODUCTION

A logarithm of a number is the exponent the base, must be raised to produce that number. For example, the logarithm of 1000 to base 10 is the exponent 3, because 10 to the power 3 is 1000: 1000 = 10 × 10 × 10 = 10^3.

Each discipline has their favorite logarithm bases that are prominent in their theories and algorithms. In computer science, it’s the binary log, or logarithm base 2. For Physicists and Engineers, many of their applications use the common log, or logarithm base 10. And, for Mathematicians, they use the natural log, or logarithm base e (Euler’s number ≈ 2.71828).

The confusion arises in the notations because there are overlapping logarithm shorthands with different meanings. Specifically, Engineers will denote the natural logarithm as \( y = \log x \) while a Mathematician interprets this as log base 10 and denotes the natural log as \( y = \ln x \).

To demonstrate the different SAS LOG functions, this paper will use the most basic identities, trivial identities:

\[
\begin{align*}
\text{LOG}_b(1) &= 0 \text{ because } b^0 = 1 \\
\text{LOG}_b(b) &= 1 \text{ because } b^1 = b
\end{align*}
\]

EXAMINING THE SYNTAX OF LOG FUNCTIONS

In SAS, there are several logarithm functions available to the programmer. It is important to know the definition of the function that you are programming to ensure proper use. As discussed earlier, Mathematicians and Engineers denote the logarithm bases differently. So, do assume the functional syntax is your discipline’s shorthand.

THE NATURAL LOG

In SAS, the function for the natural log is LOG. In Example 1, the trivial identities are tested in a DATA step. The input of 1, returns the expected value of 0 and using a Euler’s Number approximation of 2.71828, the result \( y \) is very close to 1.

In this case, we can use another SAS function to help demonstrate the LOG function. The CONSTANT function will return the value of a mathematical constant. For Euler’s Number, the proper notation is ‘E’. From reviewing the log using CONSTANT(‘E’), the expected value of 1 is returned.

To prevent more confusion, it is important to note that ‘EULER’ is also a valid input for the CONSTANT function, but this represents a different mathematical constant – Euler’s Constant or 0.5772.
THE COMMON LOG

For the common log, the SAS function is LOG10. In Example 2, the trivial identities are again programmed in a DATA step. After reviewing the log we see the expected results of 0 and 1 are returned for the inputs of 1 and 10, respectively.

OTHER LOG FUNCTIONS

Addition logarithmic functions are available in SAS beyond the natural log and common log. Among these are the LOG2 function that returns the binary logarithm, or base 2, and the LOG1PX function that returns the logarithm of one plus the argument. LOG1PX is useful when the argument is close to zero, because it is more accurate than using LOG(1+x). The juxtaposition of LOG1PX and LOG(1+x) are beyond the scope of this paper, but more information can be found in Base SAS® Language Reference.

THE EXPONENTIAL FUNCTION AND OPERATOR

Quality checks in programming are always a good idea. One way to check to make sure that the appropriate log function was used is to check the results the inverse operation using exponents. An exponential (or antilog) with the same base as the log function will undo the operation.

EXPONENTIAL FUNCTION

The EXP function raises the input argument to the power of Euler's Number, e. This can be used to check or undo the natural log function LOG.

In Example 3, the EXP function has been used to undo LOG(1), LOG(2.71828), and LOG(CONSTANT('E')). Reviewing the log, each quality check applied has returned the original argument of the LOG function.

EXPONENTIAL OPERATOR

Although the exponential function can only be used for the LOG function, the exponential operator can be used to check any logarithm base. The exponential operator is a double asterisk (**) and is used to inverse logarithm functions by taking the base of the logarithm and raising to the result of logarithm. In Output 1, the code below was run using ten test values (TEST_VALUE):

```
_LOG_  =  LOG(TEST_VALUE);
ANTILOG  =  CONSTANT('E')**_LOG_

_LOG10_  =  LOG10(TEST_VALUE);
ANTILOG10  =  10**_LOG10_

_LOG2_  =  LOG2(TEST_VALUE);
ANTILOG2  =  2**_LOG2_
```

The results show that in each pairing the ANTILOG variables match the original test value. This is a good quality check to ensure that you are using the proper base in the logarithm function.
AN APPLICATION OF LOG FUNCTIONS

Logarithms have their place in nearly every disciple from the laws of human perception to describing musical tones. However, in SAS programming a common application of log functions across industries is in the derivation of geometric means. To program a geometric mean, both the log function and its exponential inverse is used.

GEOMETRIC MEANS

Geometric mean can be used to evaluate data covering several orders of magnitude. The mathematical definition of a geometric mean is the nth root of the product of numbers. However, it's in the practical definition where logarithms are used since the average of the logarithmic values converted back to a base number will give the same result. Example 4 shows this process.

The variables _LOG_ and _LOG10_ are used from Output 1 and a PROC SUMMARY to calculate the mean. Next, the exponential inverse is programmed in a DATA step. In Output 2, GEOMEAN_LOG equals GEOMEAN_LOG10 showing that it does not matter what log base is used. Just make sure that the correct exponent inverse is applied!

CONCLUSION

There are many applications of logarithms. It is important to make sure that proper function is applied in the analysis. A function's syntax can be misleading so the programmer must be careful that the correct base is used. Having quality checks using the inverse exponential functions or operators can help ensure that the correct log function is programmed.
REFERENCES


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RECOMMENDED READING

Base SAS® Language Reference

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